

Syllabus  
**Math 01.341 - Modern Algebra II**

**CATALOG DESCRIPTION:**

**Math 01.341 Modern Algebra II, 3 s.h**

Prerequisite: Math 01.340 Modern Algebra I with a grade of C- or better

This course extends the study begun in Modern Algebra I to a more detailed investigation of abstract algebraic structures. Included are Sylow theorems, rings and ideals, polynomial rings, ring and field extension and Galois Theory.

**CONTENT:**

**1. Group Theory**

- 1.1 Normal subgroup
- 1.2 Fundamental Theorem of Groups (Quotient Group)
- 1.3 Group isomorphism theorems
- 1.4 Cauchy's Theorem for abelian groups
- 1.5 Group automorphisms
- 1.6 Cayley's Theorem
- 1.7 Permutation groups
- 1.8 Sylow Theorems

**2. Ring Theory**

- 2.1 Ideal and prime ideals
- 2.2 Euclidean rings and principle ideal rings
- 2.3 Polynomials and zeros of a polynomial
- 2.4 Polynomial factorization theorem
- 2.5 Irreducibility criteria
- 2.6 Symmetric functions

**3. Theory of Fields**

- 3.1 Subfields and prime fields
- 3.2 Field adjunction
- 3.3 Simple field extensions
- 3.4 Linear dependence over a skew field
- 3.5 Linear equations over a skew field

- 3.6 Algebraic field extensions
- 3.7 Normal extension fields
- 3.8 Roots of unity
- 3.9 Finite commutative fields (Galois fields)
- 3.10 Separable and inseparable extensions
- 3.11 Perfect and imperfect fields

**TEXTS:**

Joseph Gallian, CONTEMPORARY ABSTRACT ALGEBRA, 6<sup>th</sup> ed, Houghton Mifflin

Rotman, J.J., A FIRST COURSE IN ABSTRACT ALGEBRA, 2<sup>nd</sup> ed, Prentice Hall, 2000

Pinter, C.C., A BOOK OF ABSTRACT ALGEBRA, 2<sup>nd</sup> ed, Dover, 1990

Herstein, I.N., TOPICS IN ALGEBRA, 2<sup>nd</sup> ed., Xerox, Mass., 1975

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