## Mathematics Department Colloquium

**Speaker:** Dr. Rachel L. Petrik, Department of Mathematics, University of Kentucky, Lexington

**Title:** Solutions to Systems of Equations over Finite Fields

Date: Monday December 9, 2019

**Time:** 2:00pm to 3:00pm.

Place: James Hall 2100

**Abstract:** Solving systems of equations is among the most classical mathematical problems. In number theory, we are particularly interested in integer solutions to systems of equations. A necessary condition for the existence of an integer solution is the existence of a solution over the finite field,  $F_p$ , for every prime p. In the study of systems of polynomials over finite fields, there are typically three questions one can ask.

- 1. Can we find and describe all solutions?
- 2. How many solutions are there?
- 3. When does there exist at least one solution?

In this talk, I will introduce some classical results in the area and then discuss my contributions to the field, including my improvements to the Chevalley-Warning bounds.